

High Speed Propulsion

KTH Rocket Course 2008

Ulf.Olsson.Thn @Telia.com



AEROSPACE PROPULSION FROM INSECTS TO SPACEFLIGHT

Ulf Olsson



COMPUTERIZED EDUCATIONAL PLATFORM
HEAT AND POWER TECHNOLOGY
Lecture Series Volume No.3

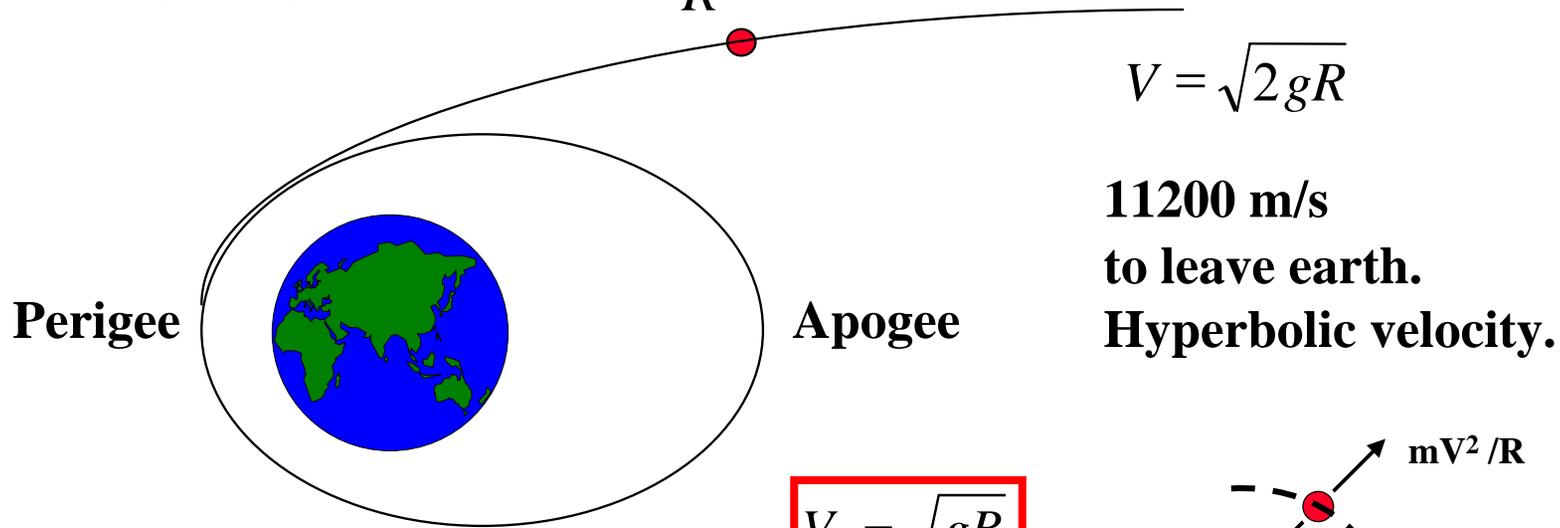
STOCKHOLM 2006

What velocities?



Isaac Newton:
Law of gravity 1687

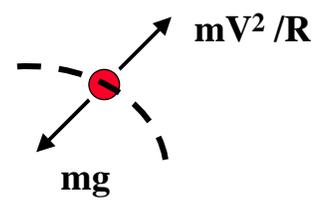
$$g = g_0 \frac{R_0^2}{R^2}$$

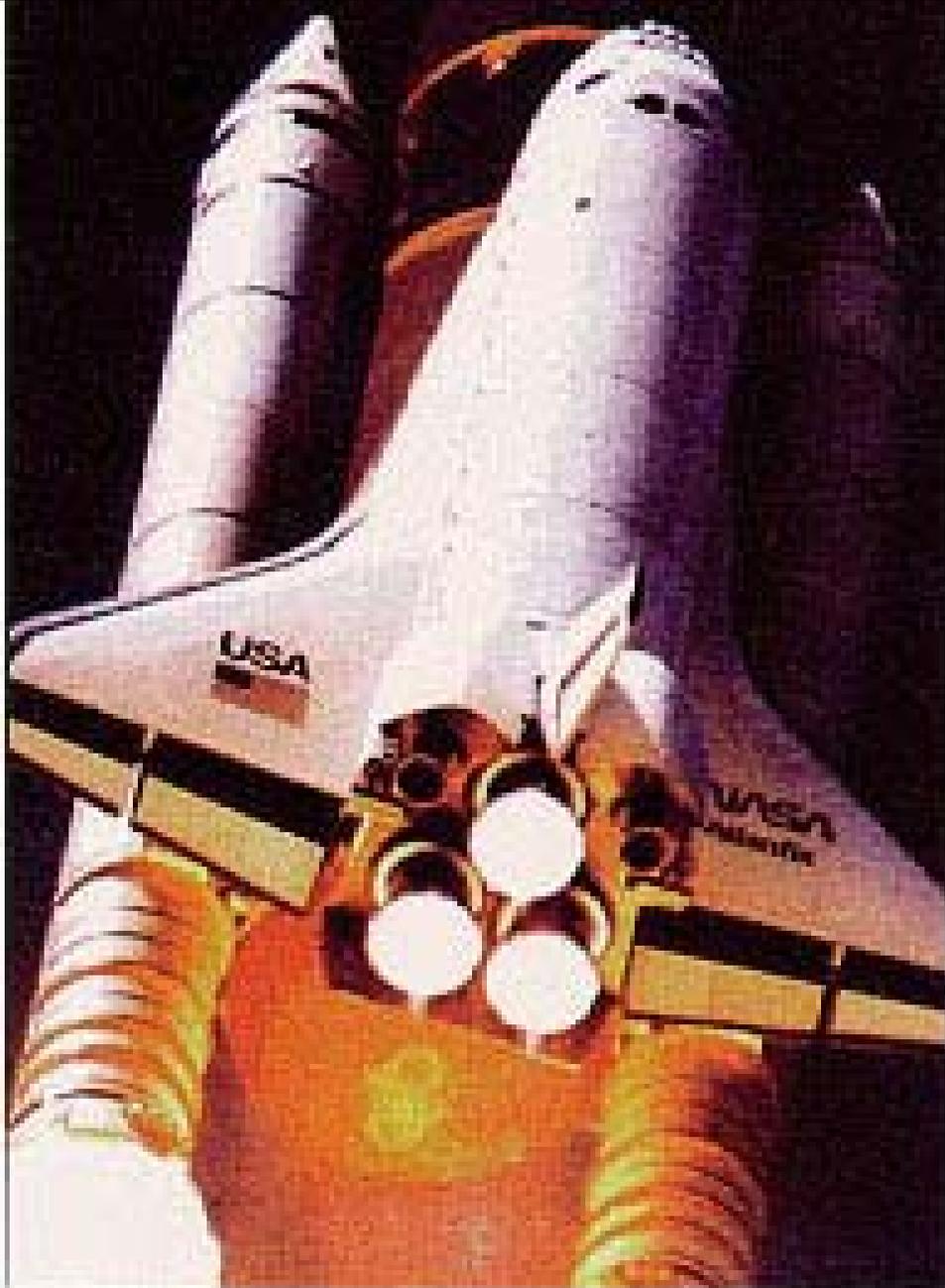


$V = \sqrt{2gR}$
11200 m/s
to leave earth.
Hyperbolic velocity.

$$V_0 = \sqrt{gR}$$

Circular velocity 7900 m/s.
Mach 26.





**The spaceplane would give more flexible space access.
(Eugen Sänger and Irene Bredt 1944).**



Wings and atmospheric oxygene

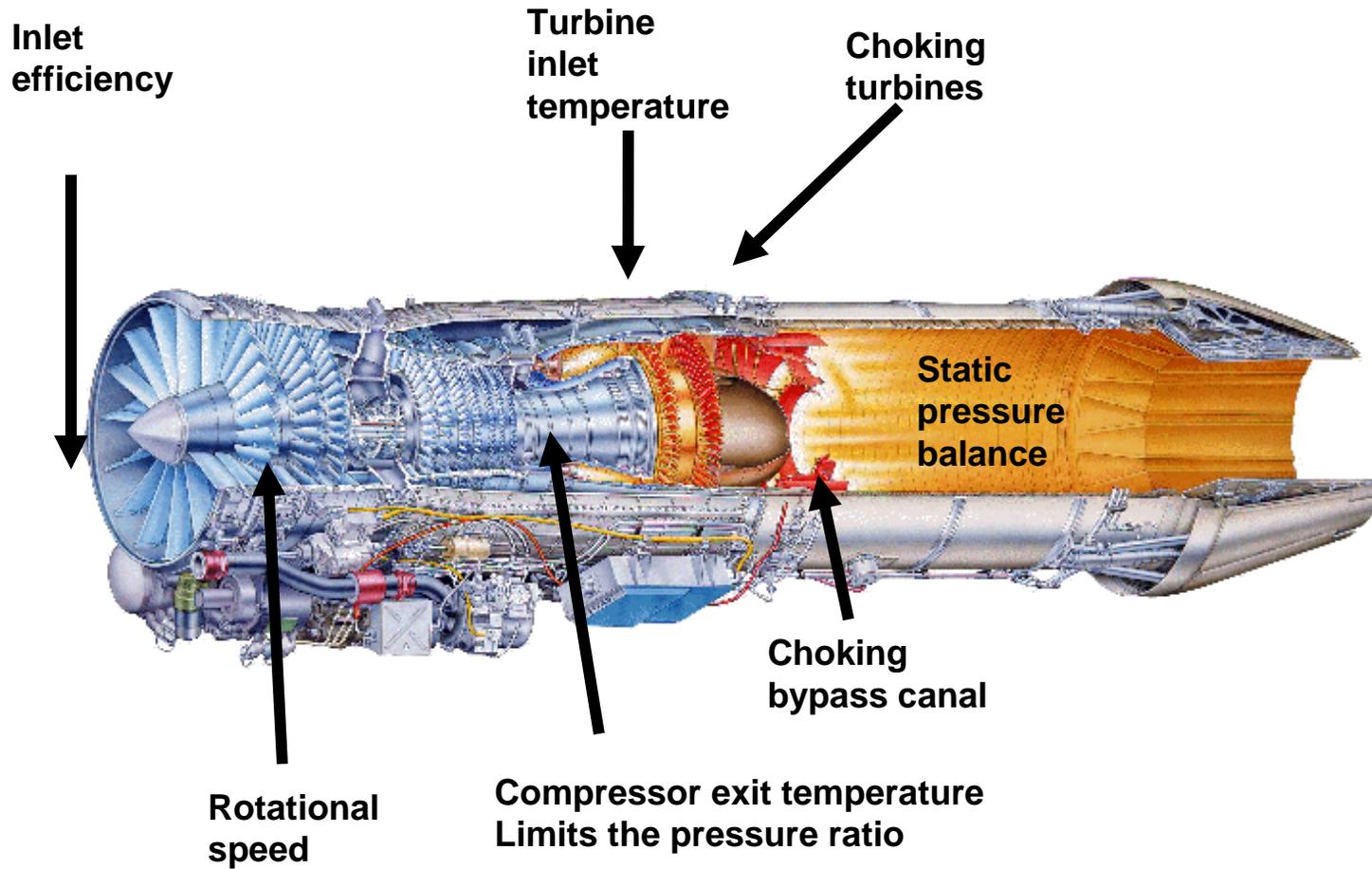
The SR71- the highest speed aircraft ever (Mach 3.2)



The limits of the turbojet engine $F = \dot{m}(V_j - V)$

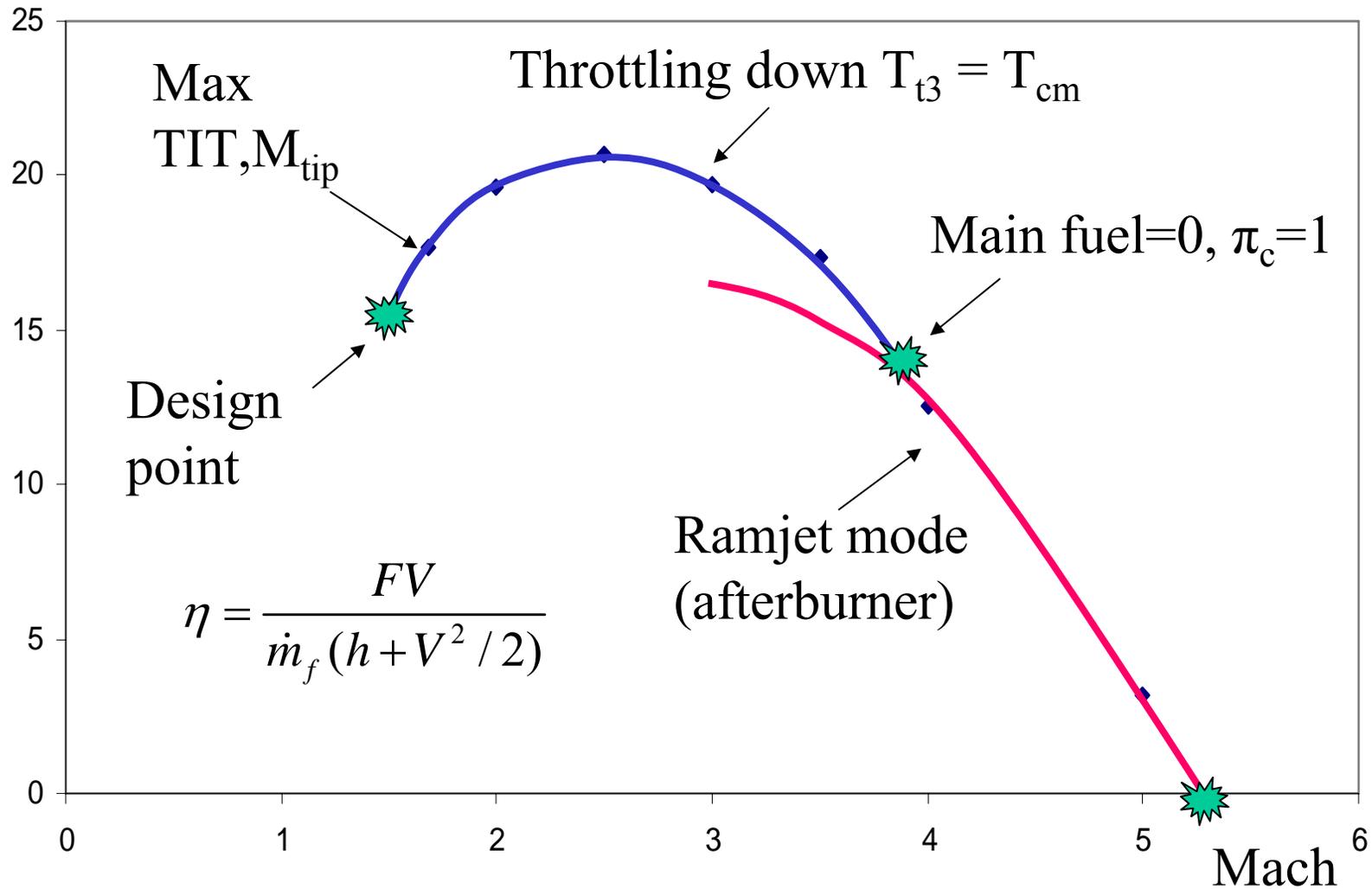
The turbine inlet temperature limits the thrust.

$$\frac{F}{\dot{m}a_0} = \sqrt{\frac{2}{\gamma - 1}} (\sqrt{T_{t4} / T_0} - 1)$$



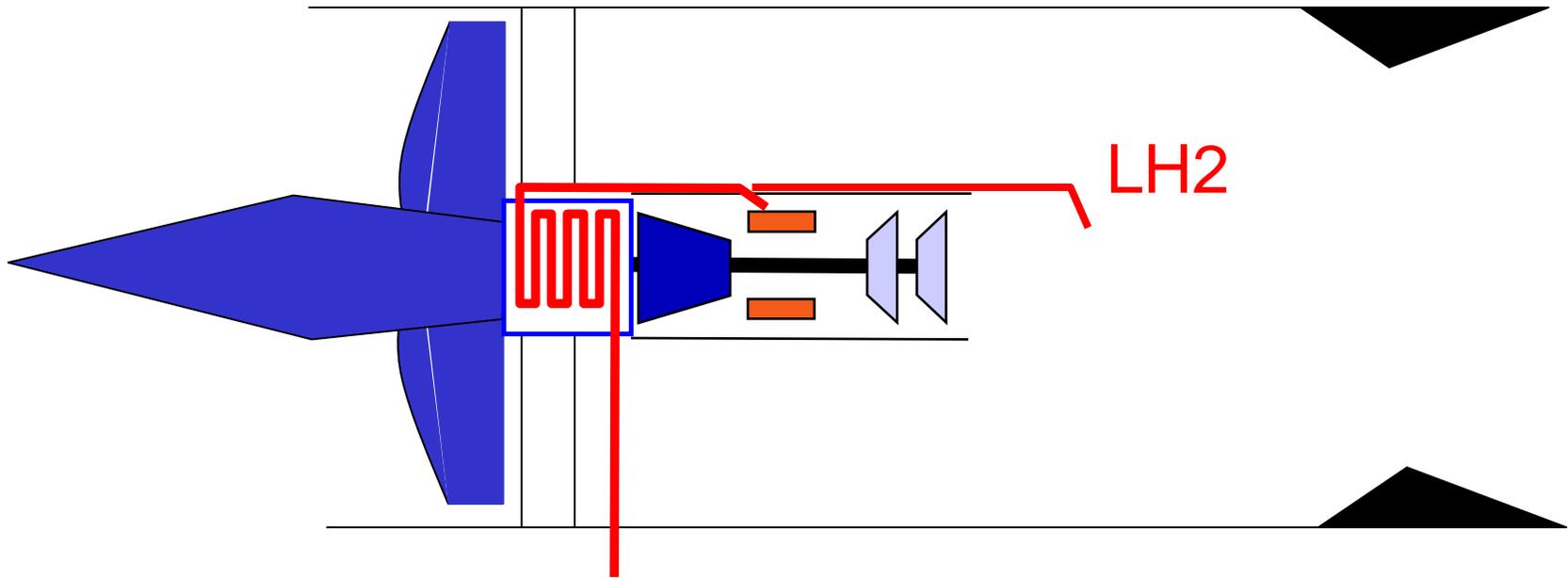
Efficiency %

Turboramjet



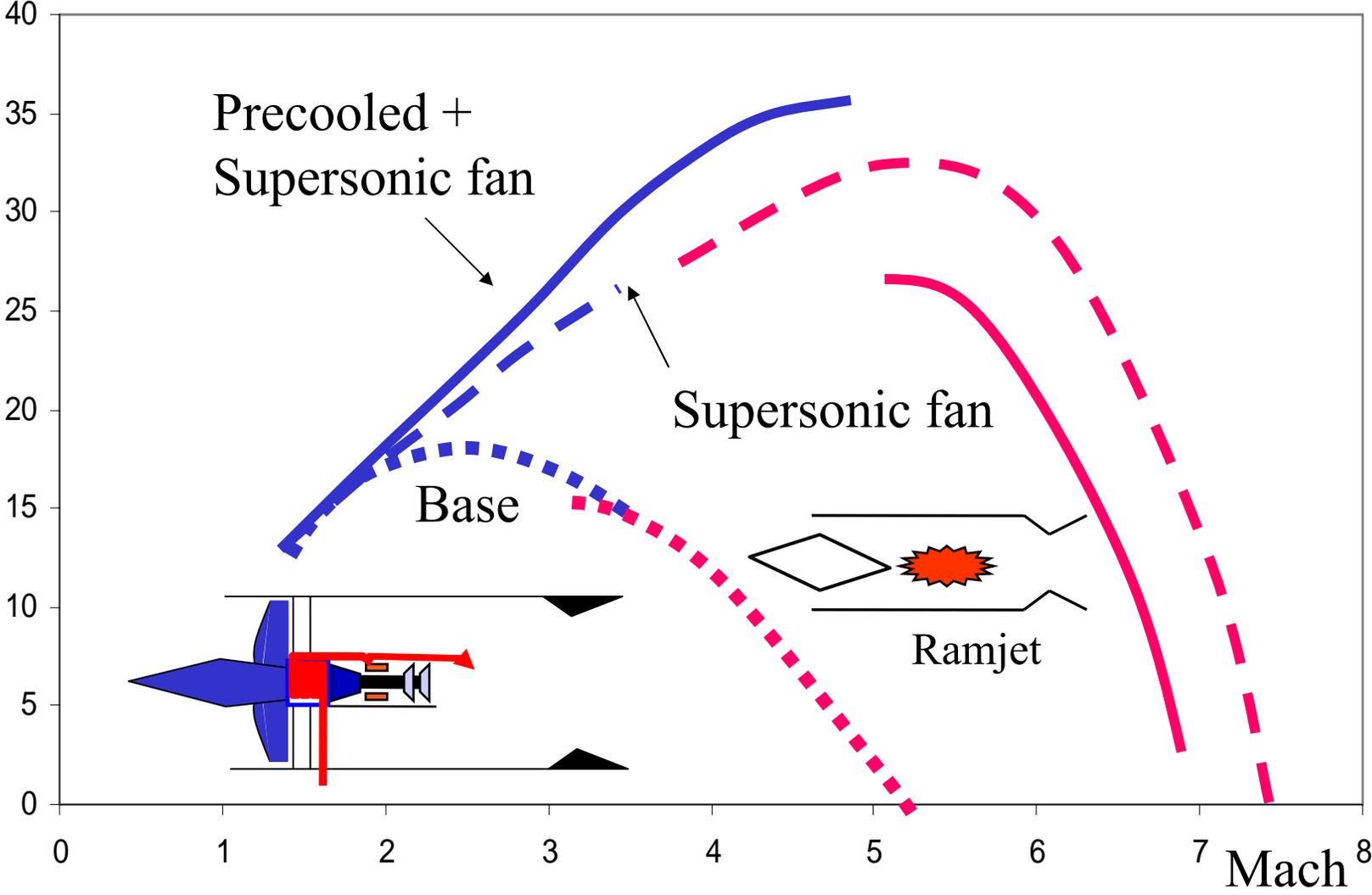
Close down the turbomachine at high speed

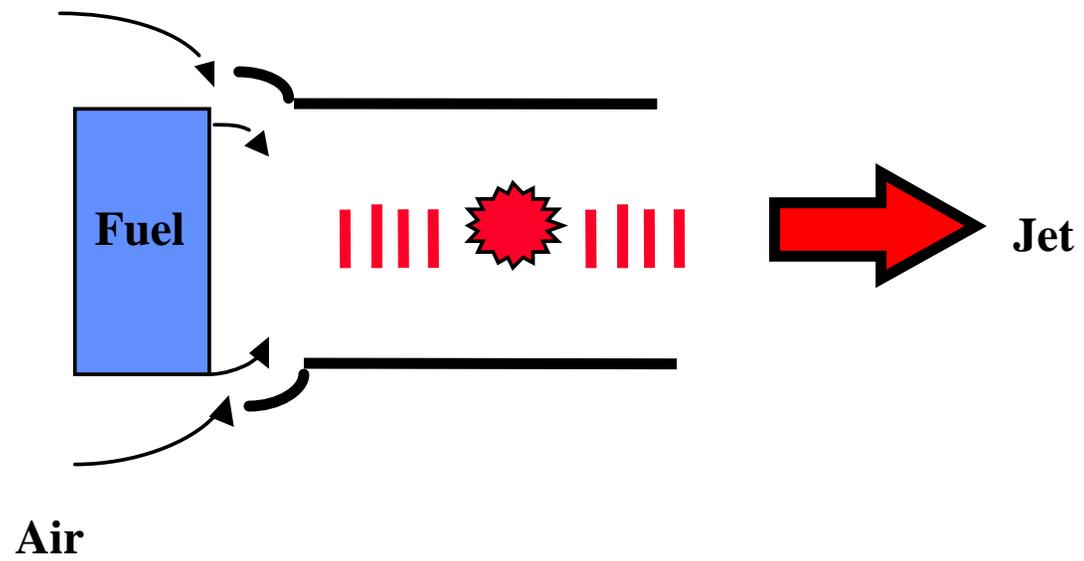
Supersonic fan for less inlet losses



Precooling for extended turbojet operation

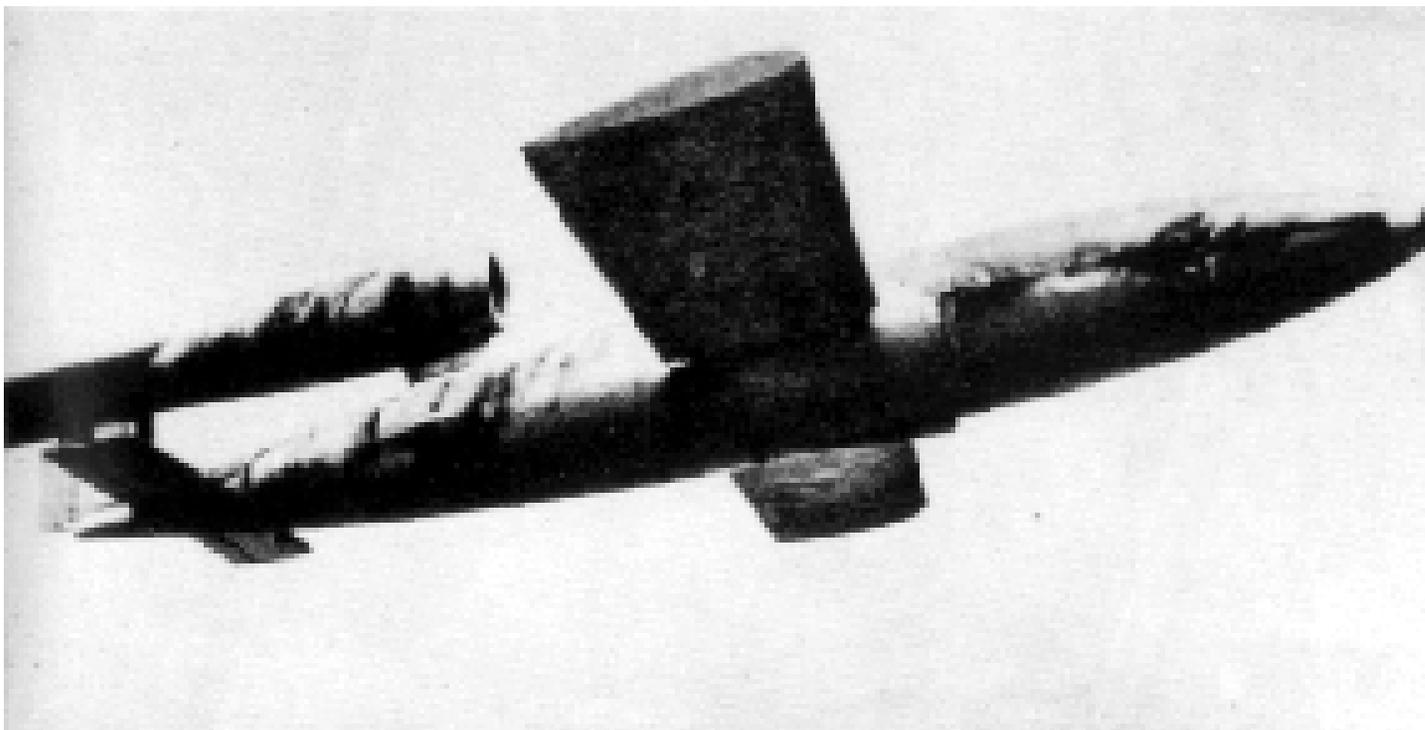
Efficiency %

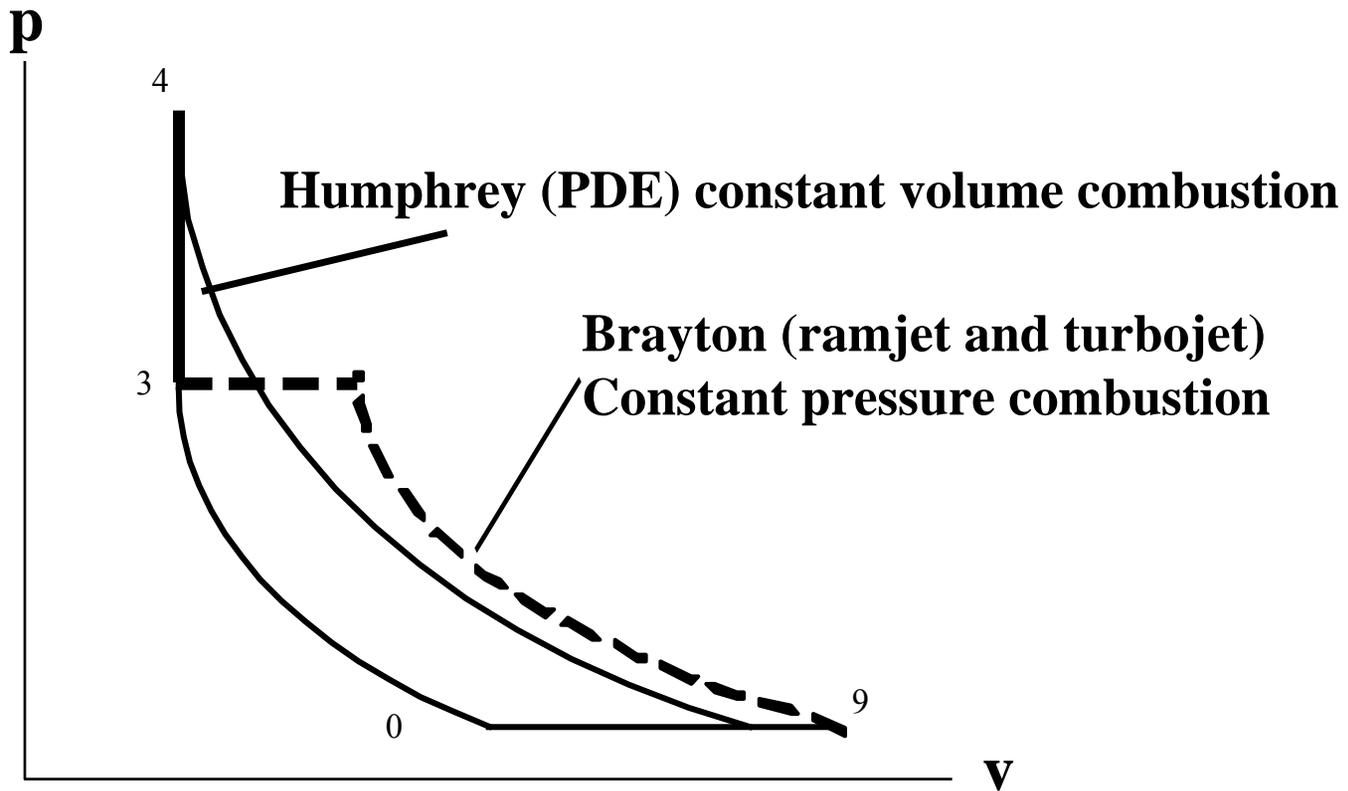




The principle of a Pulse Detonation Engine (PDE)

V1-German WW1 pulsejet





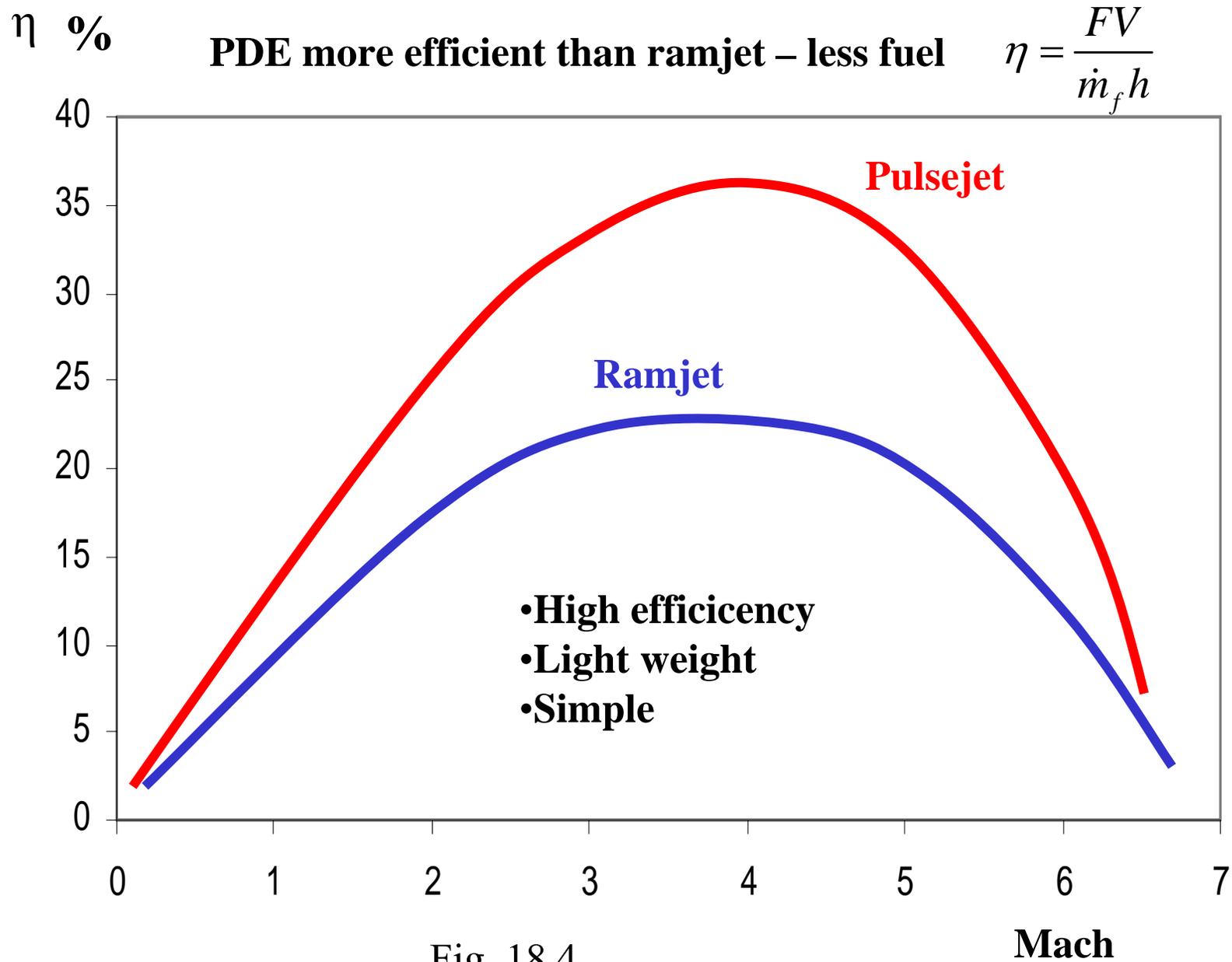


Fig. 18.4

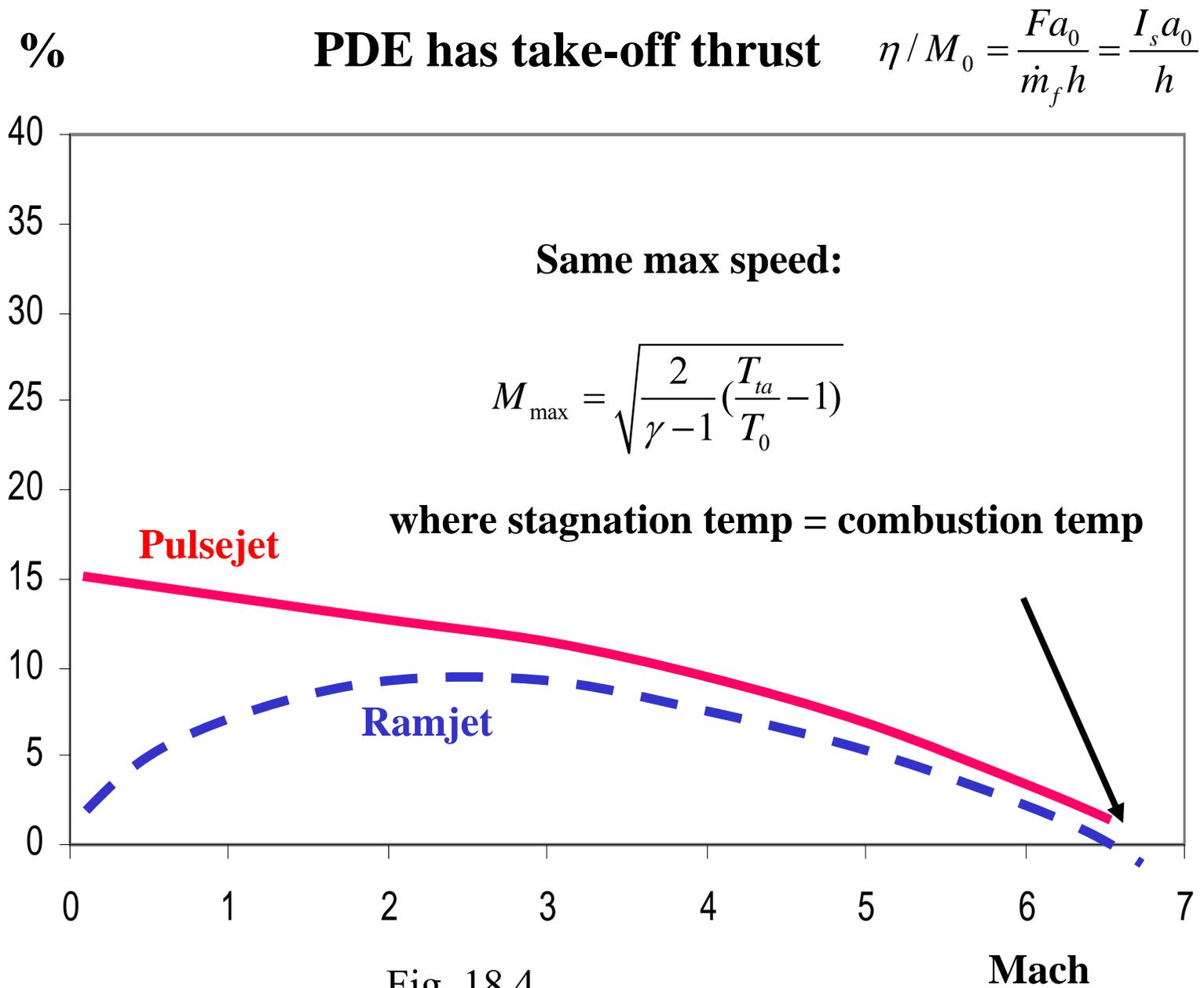
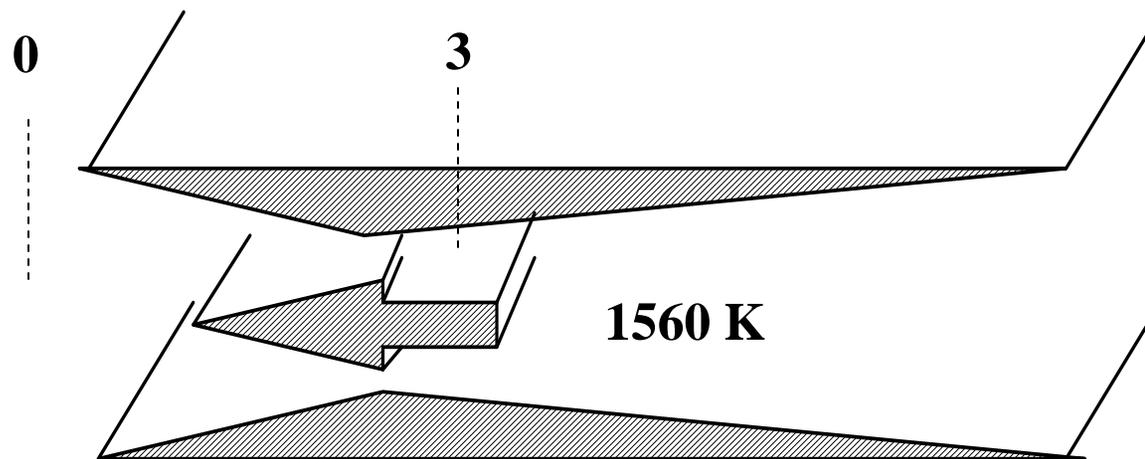


Fig. 18.4

The idea of the scramjet

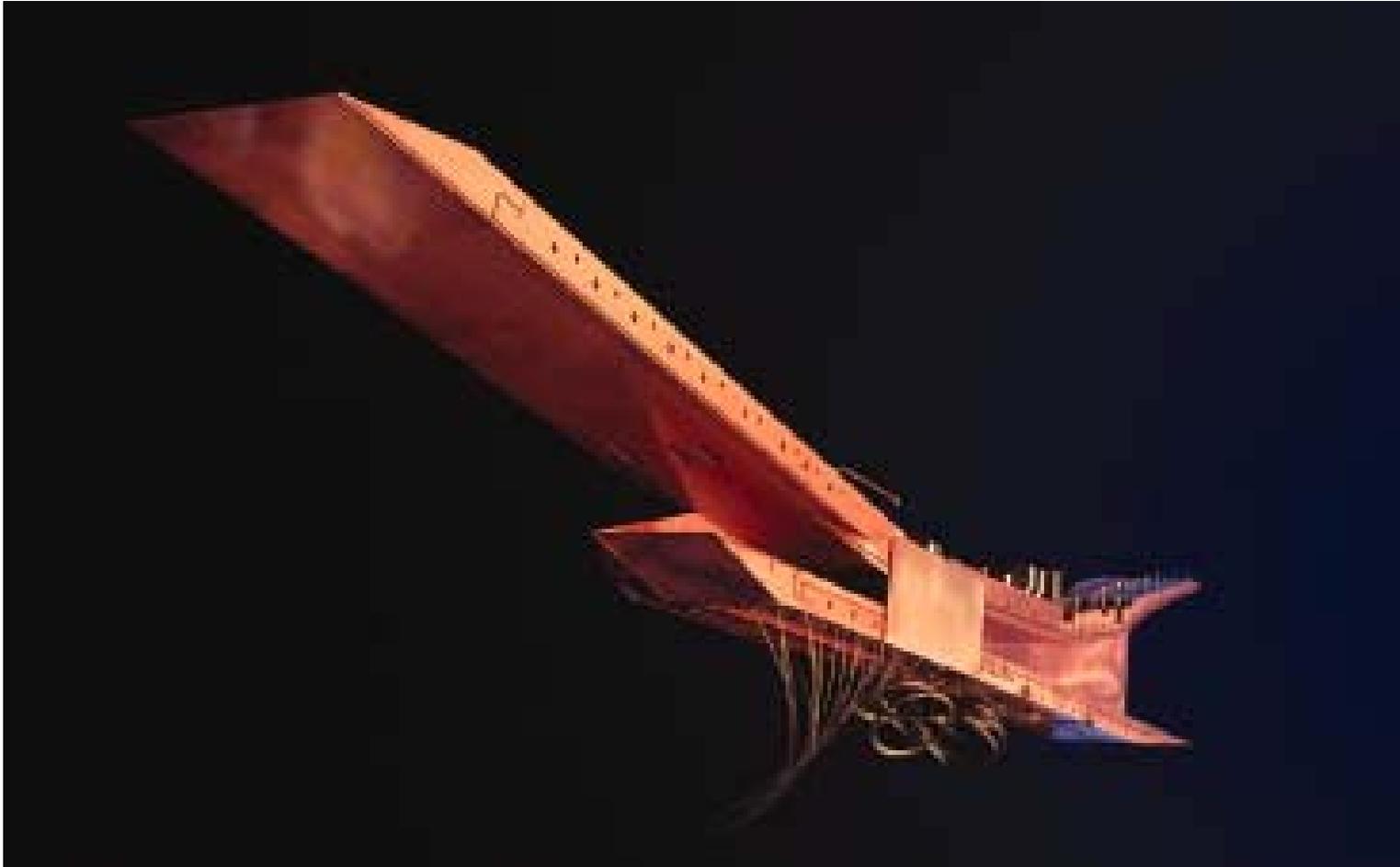
Increase M_3 to keep T_3 low to prevent dissociation (1560 K)

$$T_t = T_0 \left(1 + \frac{\gamma - 1}{2} M_0^2 \right) = T_3 \left(1 + \frac{\gamma - 1}{2} M_3^2 \right)$$

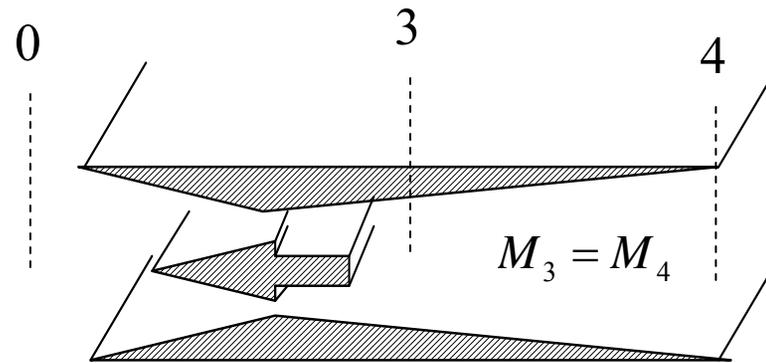


Scramjet $M_3 > 1$ if $M_0 > \sqrt{\frac{2}{\gamma - 1} \left[\left(\frac{\gamma + 1}{2} \right) \frac{T_3}{T_0} - 1 \right]}$ =6

US scramjet test hardware



The jet speed of a scramjet



**Constant Mach
in combustor**

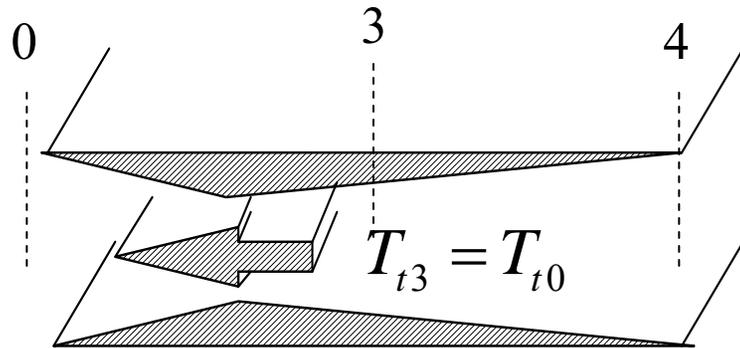
Kinetic efficiencies

$$V_3 = V_0 \sqrt{\eta_{ki}}$$

$$\frac{V_4}{V_3} = \frac{M_4 a_4}{M_3 a_3} = \sqrt{\frac{T_4}{T_3}} = \sqrt{\frac{T_{t4}}{T_{t3}}}$$

$$V_j = V_0 \sqrt{\frac{T_{t4}}{T_{t3}} \eta_{ki} \eta_{kc} \eta_{kn}}$$

The scramjet performance



Jet speed:

$$V_j = V_0 \sqrt{\frac{T_{t4}}{T_{t3}} \eta_{ki} \eta_{kc} \eta_{kn}}$$

Note max stoich $f=0.0291$ for hydrogen

Heat release: $(1 + f) C_p T_{t4} - C_p T_{t3} = \eta_b f h$

Specific thrust: $\frac{F}{\dot{m}} = (1 + f) V_j - V_0$

There is a max flight speed of the scramjet at $F=0$

The maximum Mach number of the scramjet

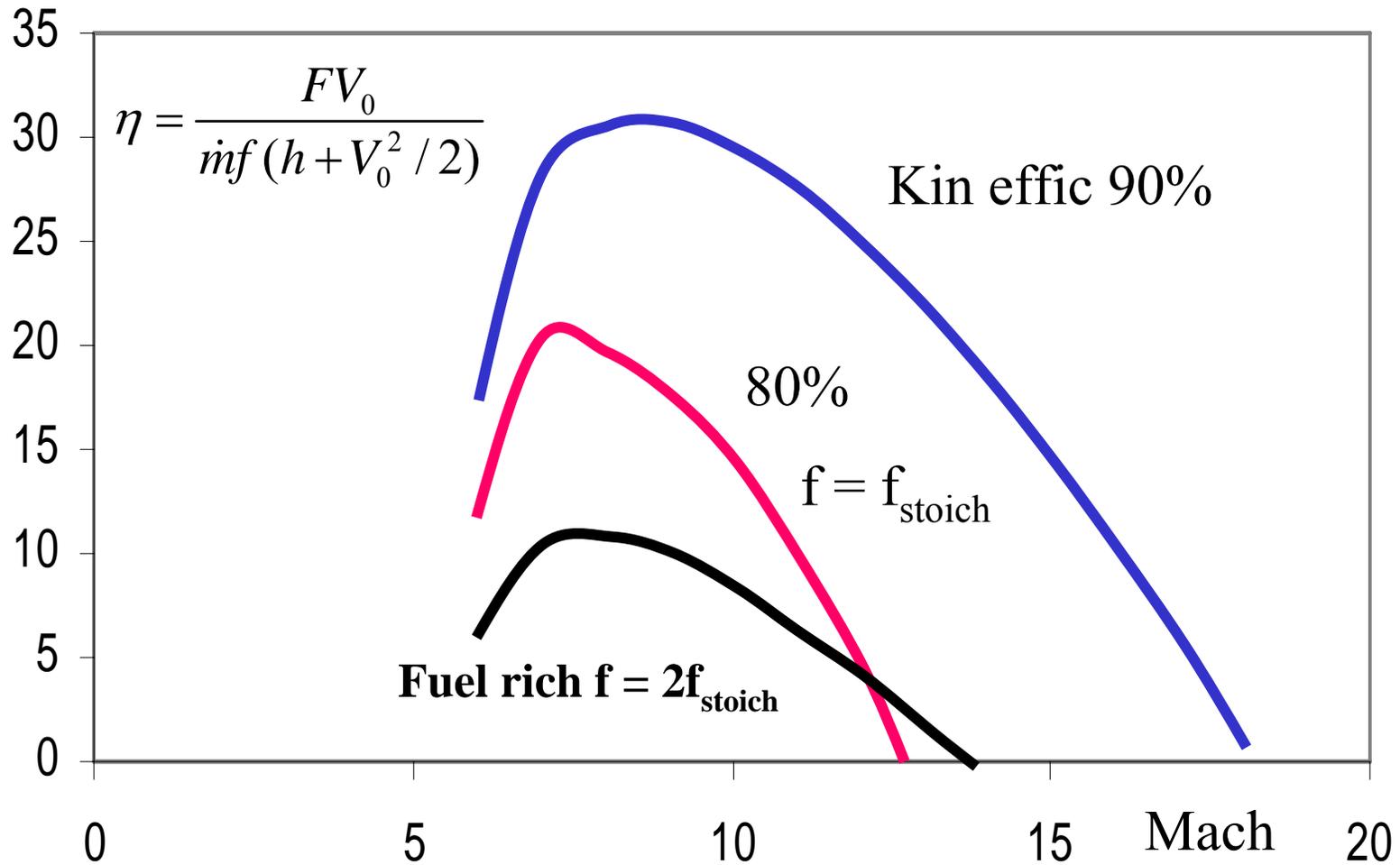
F=0 at:

$$M_{\max} = \sqrt{\frac{2}{\gamma-1} \left[\frac{\eta_b h f_s}{C_p T_0} \frac{\eta_{\text{ke}} (1+f)}{1-\eta_{\text{ke}} (1+f)} - 1 \right]}$$

Kinetic efficiency 65-75% gives max Mach number 10-15.

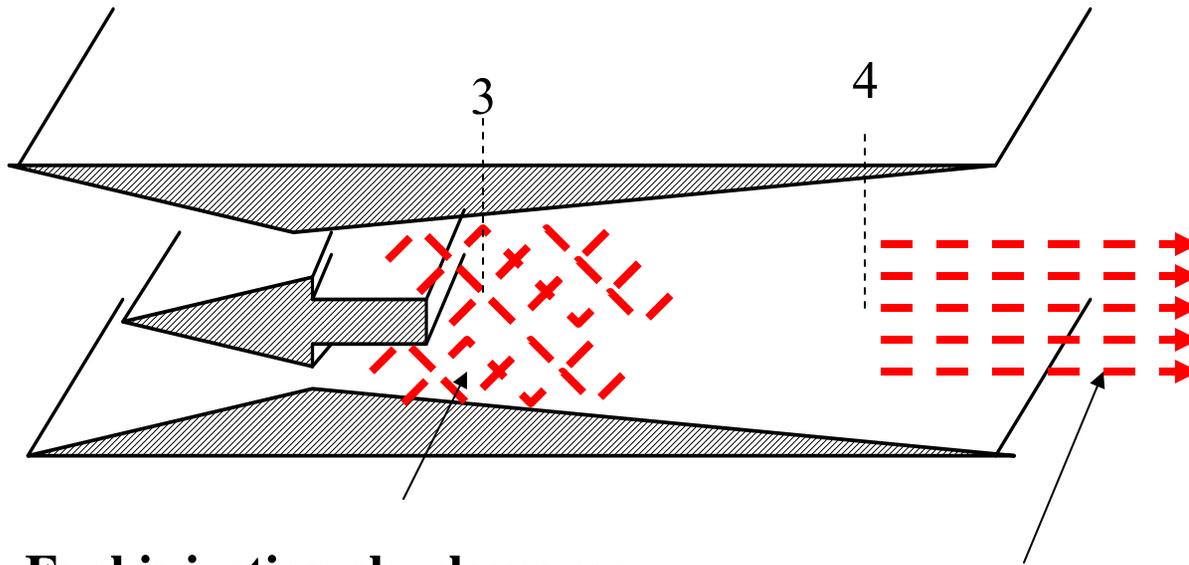
Run fuel rich to reach a higher Mach number:

% The scramjet functions between Mach 6 and Mach 15



The efficiency of a Scramjet

Problems with the scramjet



Fuel injection shock waves

Incomplete combustion

Note: $\frac{M_3}{M_0} \approx \sqrt{\frac{T_0}{T_3}}$

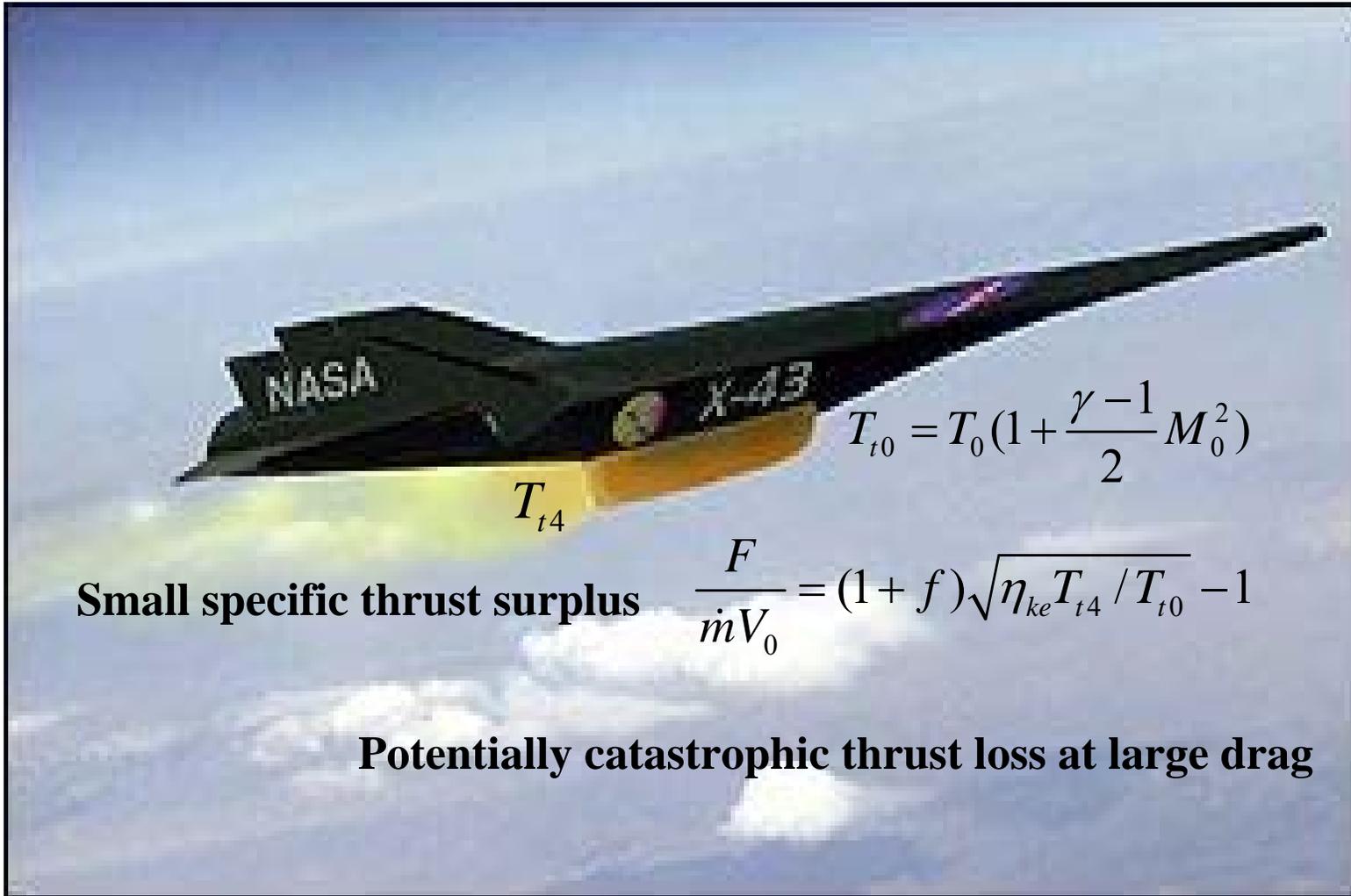
High combustor Mach numbers

Very sensitive to kinetic efficiencies $V_j = V_0 \sqrt{\frac{T_{t4}}{T_{t3}} \eta_{ki} \eta_{kc} \eta_{kn}}$

Scramjet powered spaceplane

Large intake with variable geometry





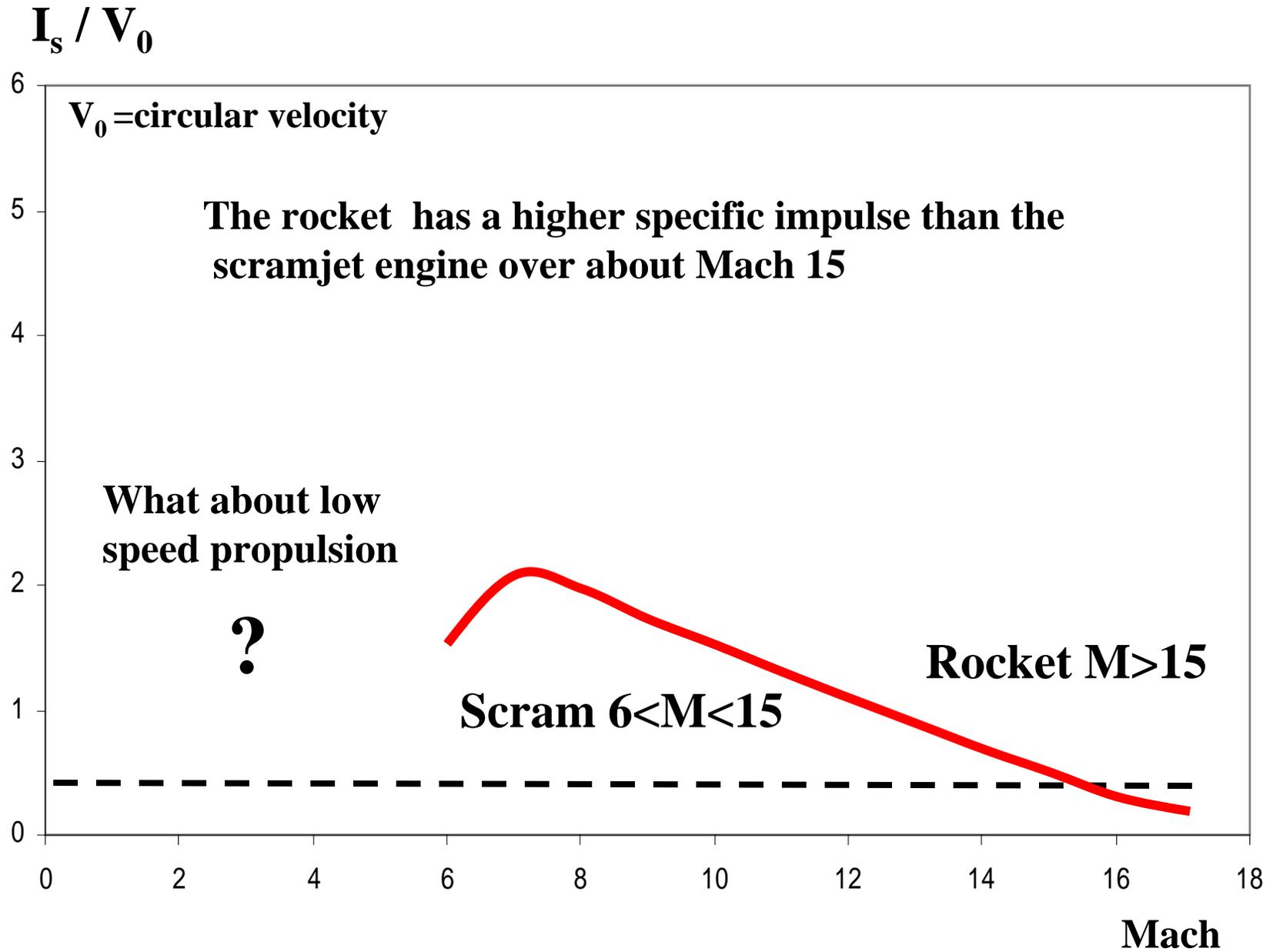
T_{t4}

$$T_{t0} = T_0 \left(1 + \frac{\gamma - 1}{2} M_0^2 \right)$$

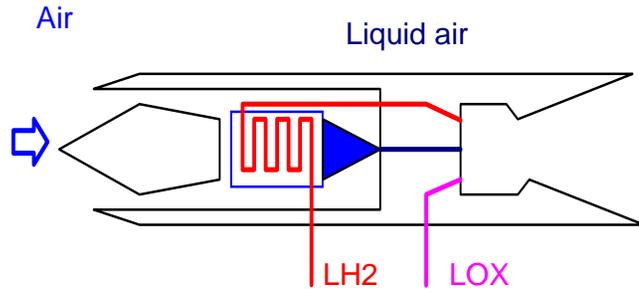
Small specific thrust surplus

$$\frac{F}{\dot{m}V_0} = (1 + f) \sqrt{\eta_{ke} T_{t4} / T_{t0}} - 1$$

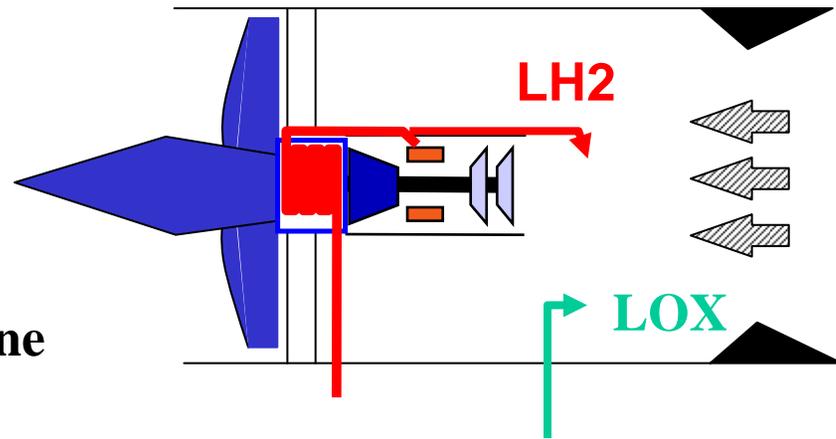
Potentially catastrophic thrust loss at large drag



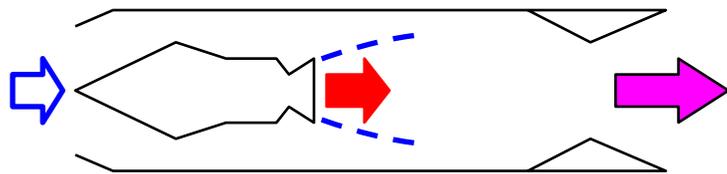
Combined engines



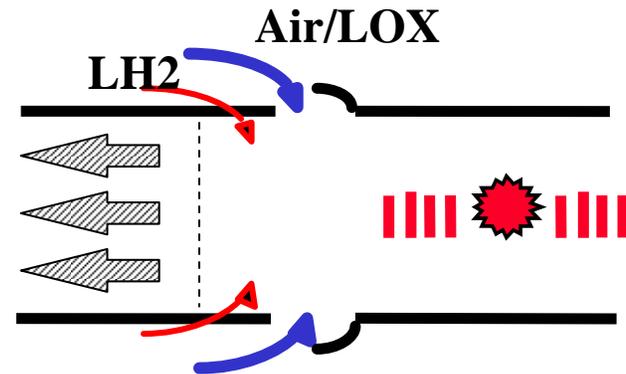
LACE-Liquid Air Combustion Engine



Precooled turboram-rocket



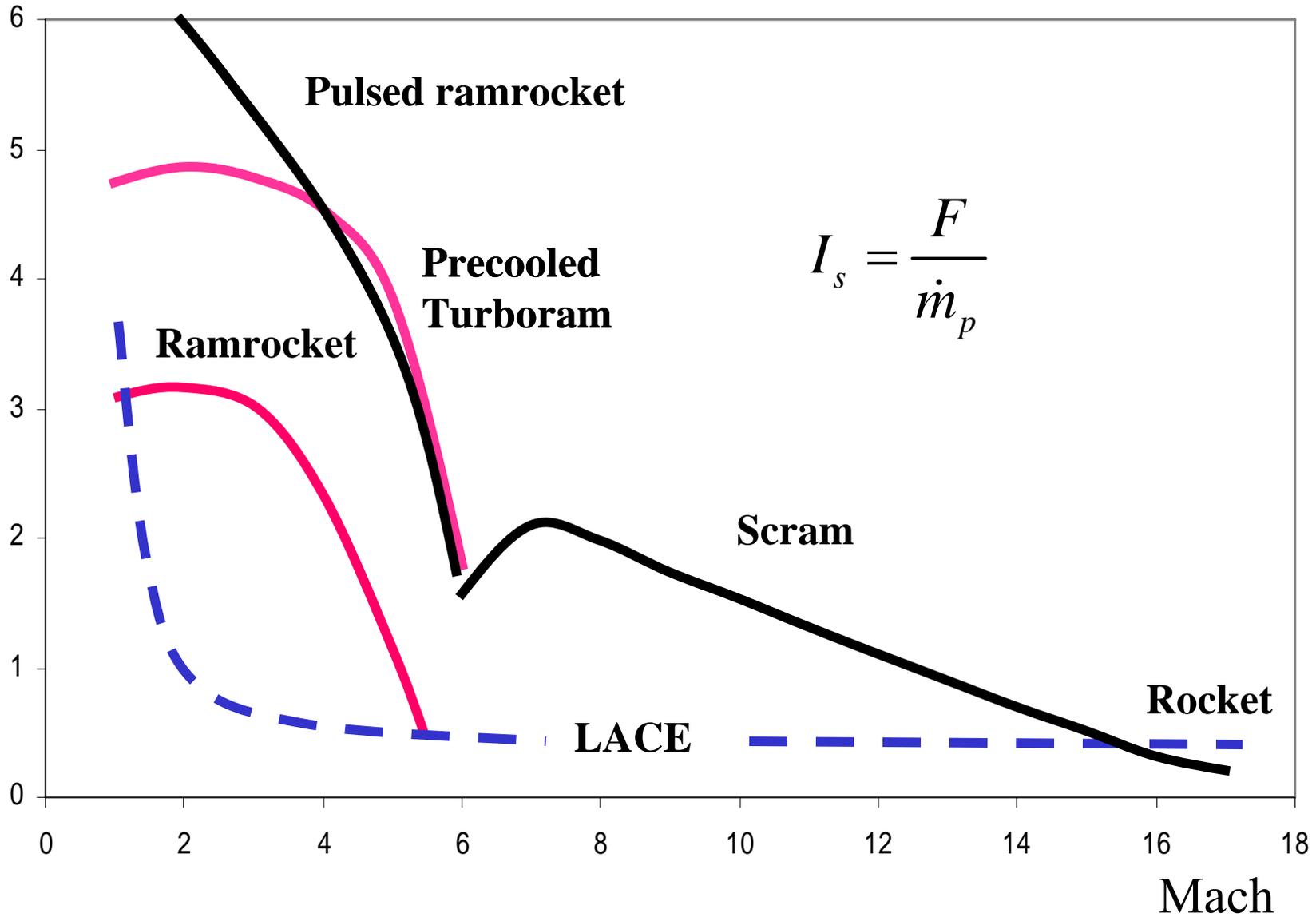
Ramrocket



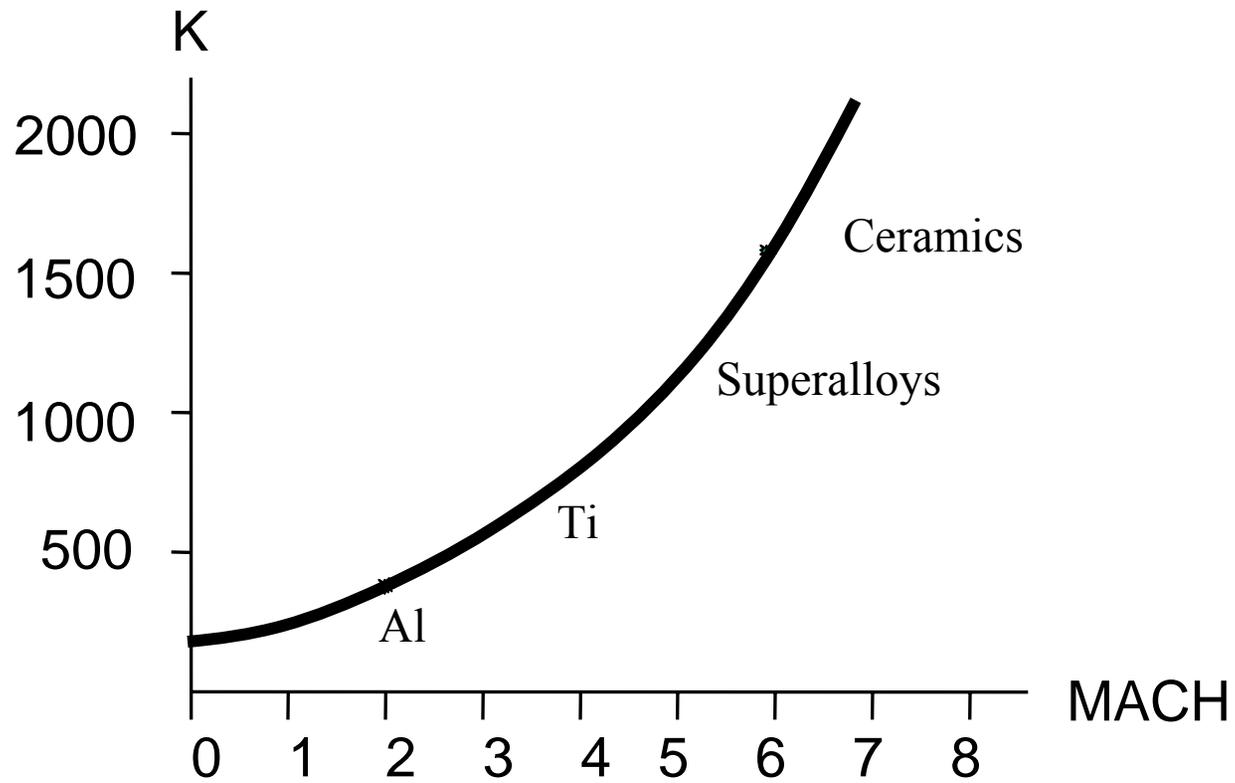
Pulsed ramrocket

I_s / V_0

Specific impulse for spaceplanes

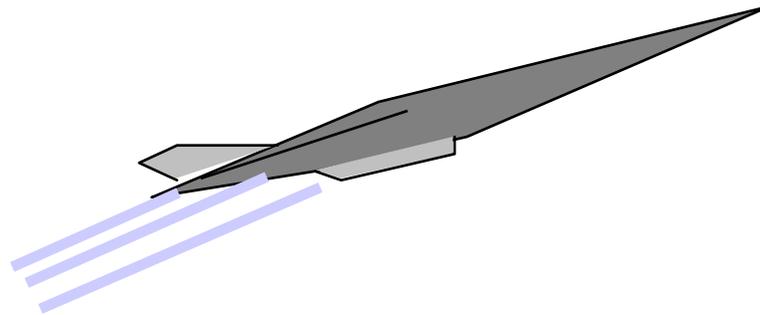


Heat protection is a big problem

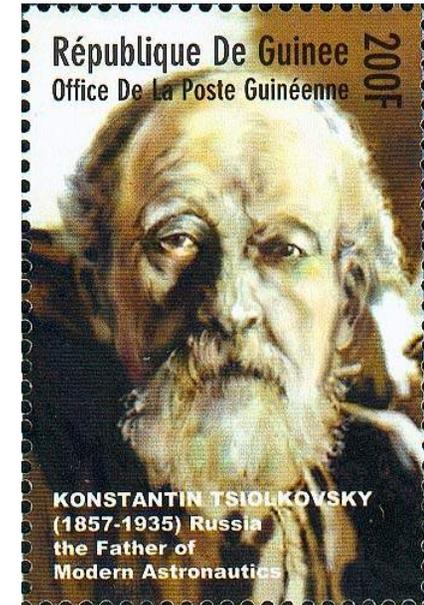


Stagnation temperature and materials

Tsiolkovsky equation with gravity and atmosphere



Ordinary Tsiolkovsky: $\frac{m_c}{m_0} = e^{-V/I_s}$



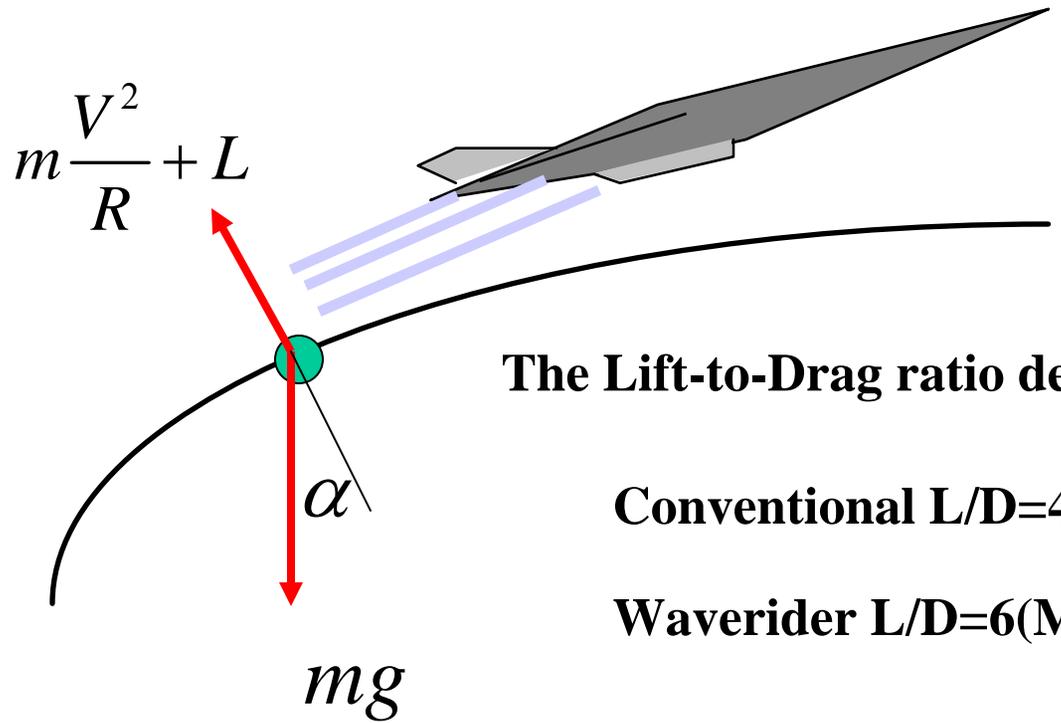
Modified for aero and gravity losses:

$$\frac{m_c}{m_0} = 1 - \frac{m_p}{m_0} = \exp\left(-\int_0^V \frac{dV}{\eta_f I_s}\right)$$

Flight efficiency

Konstantin Tsiolkovsky

Flight efficiency



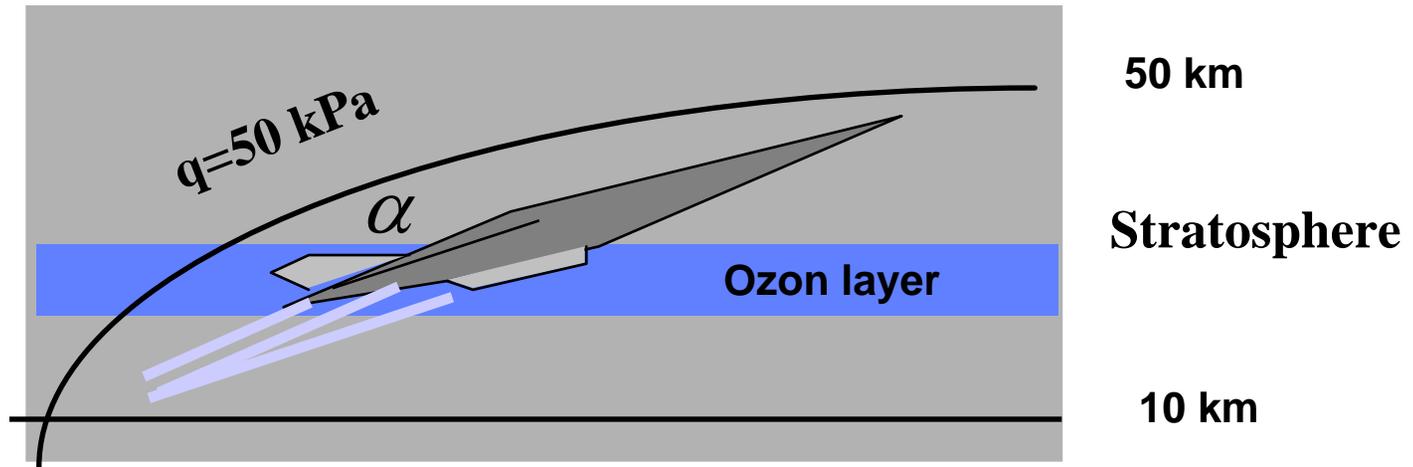
The Lift-to-Drag ratio decreases with speed

Conventional $L/D=4(M+3)/M$

Waverider $L/D=6(M+2)/M$

$$\eta_f = 1 / \left(1 + \frac{D}{L} \left(\cos \alpha - \frac{V^2}{gR} \right) \frac{g}{a} + \frac{g}{a} \sin \alpha \right)$$

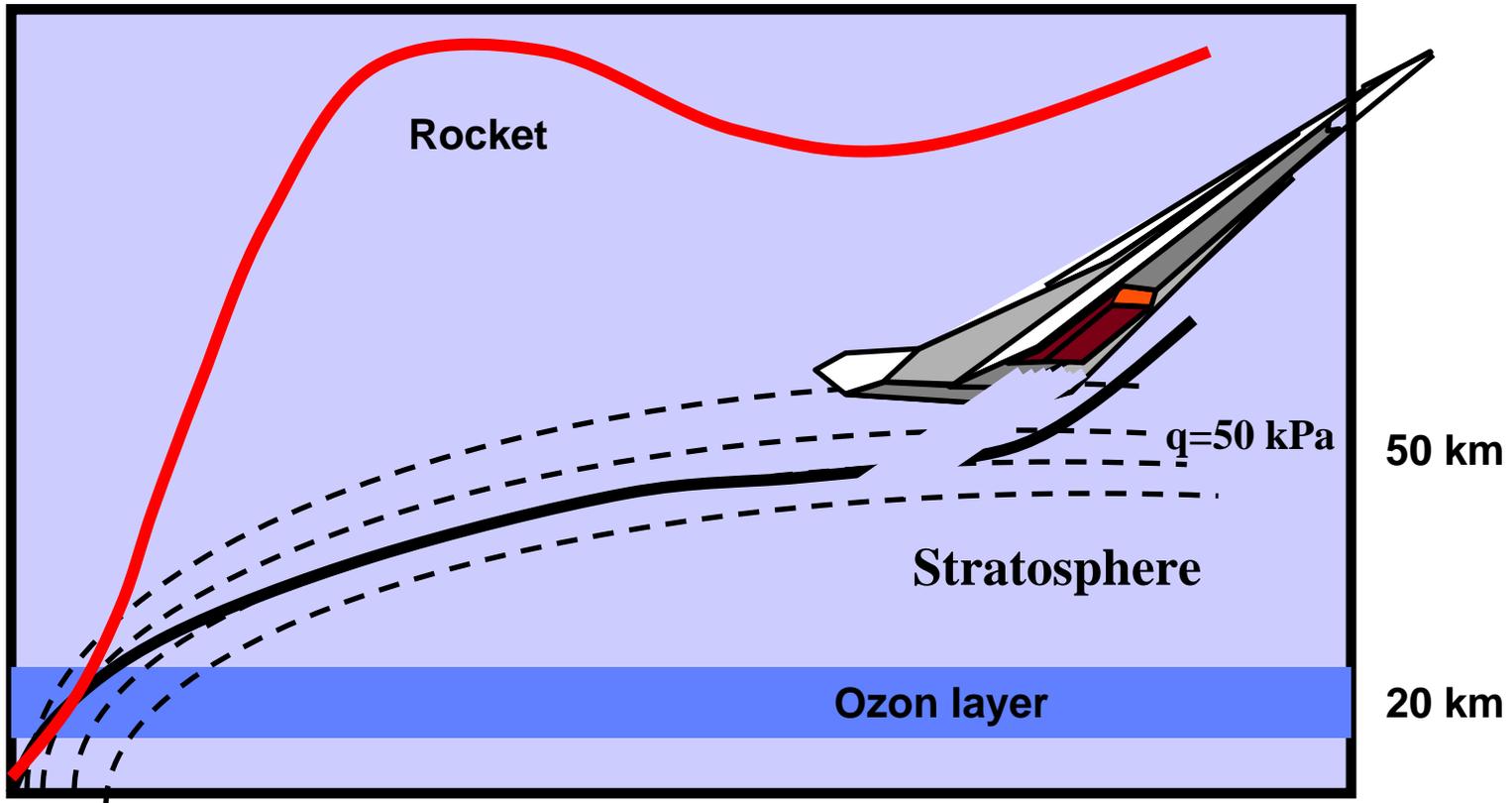
Spaceplane trajectory



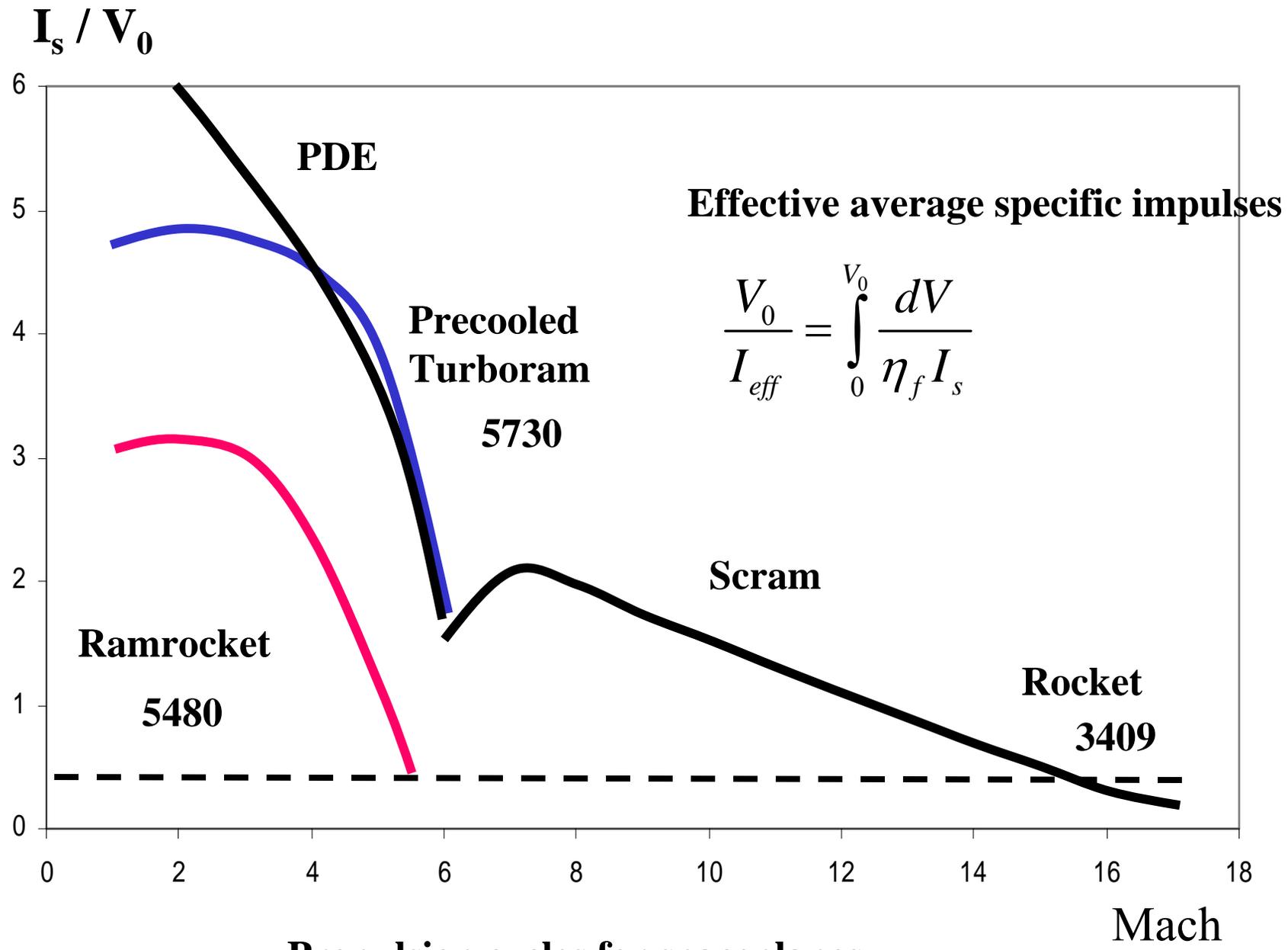
Atmospheric pressure: $\frac{p}{p_{sl}} = e^{-h/h_0}$ $h_0 = 6670 \text{ m}$

$$q = \frac{1}{2} \rho V^2 = \frac{1}{2} \frac{p}{RT} V^2 = \frac{\gamma p}{2} M^2 \quad M = \sqrt{\frac{2q}{\gamma p_{sl} e^{-h/h_0}}}$$

Flight at constant dynamic pressure q



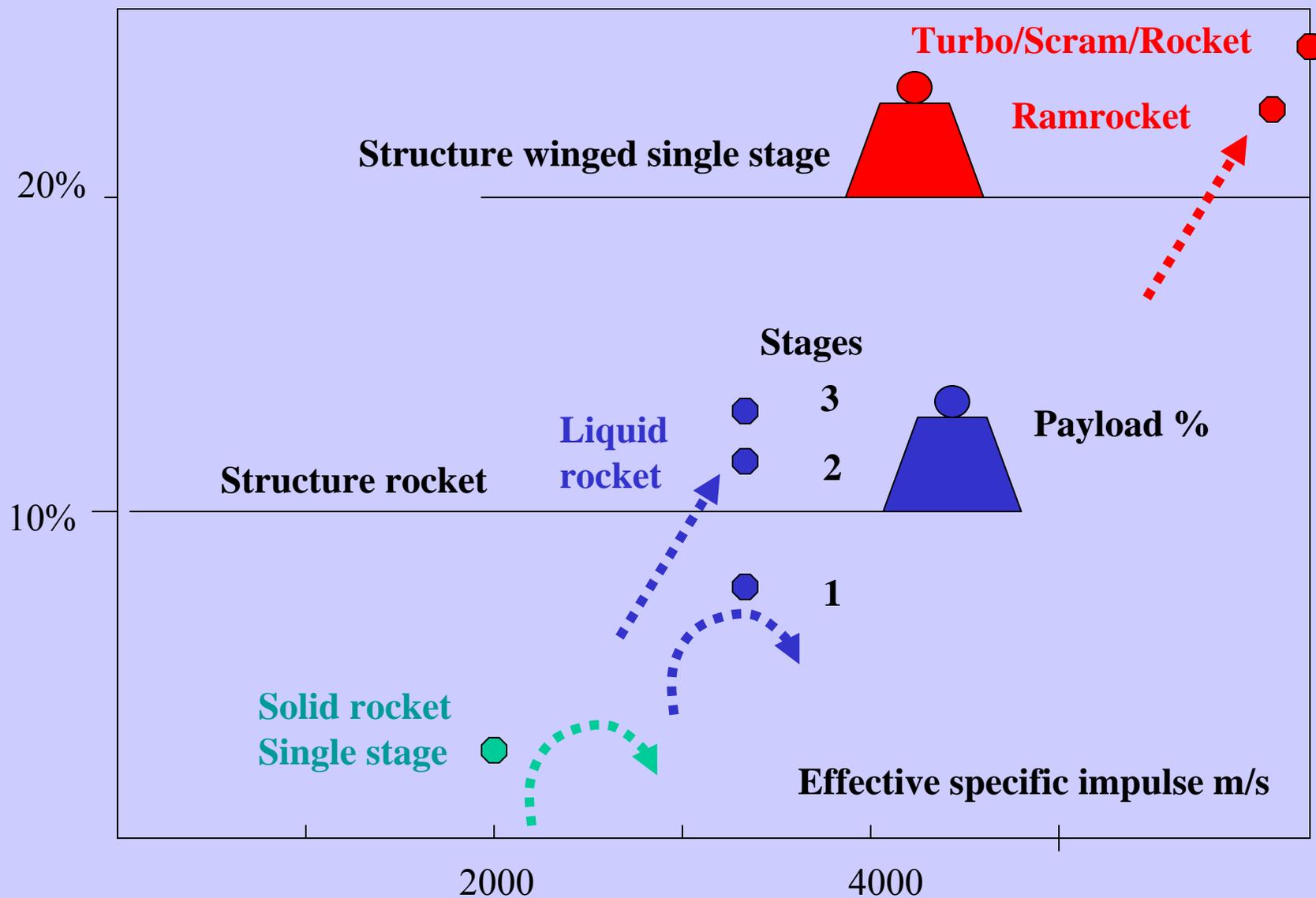
Spaceplane and rocket trajectories



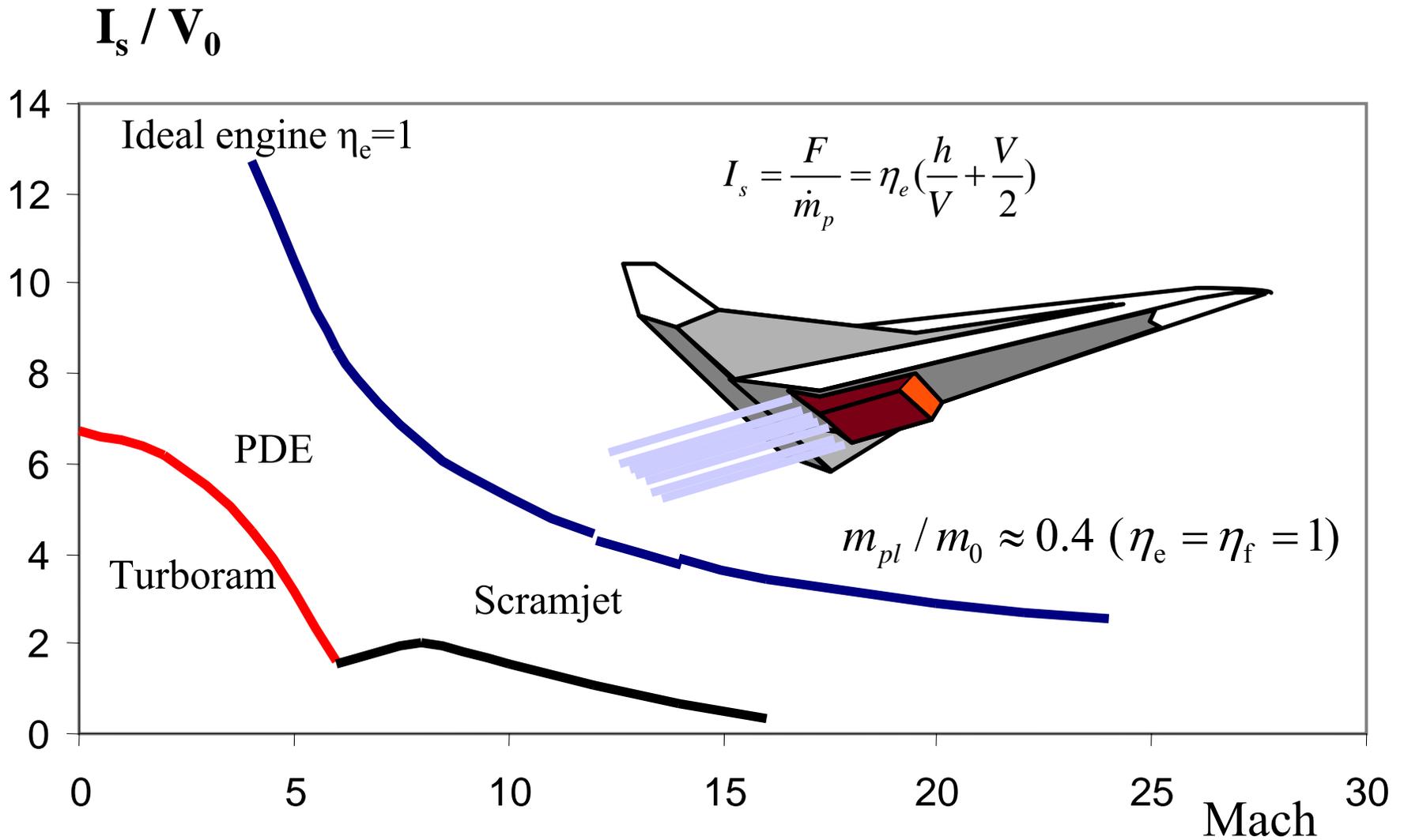
Propulsion cycles for spaceplanes

% take-off weight to satellite orbit

$$m_c / m_0 = e^{-V_0 / I_{eff}}$$



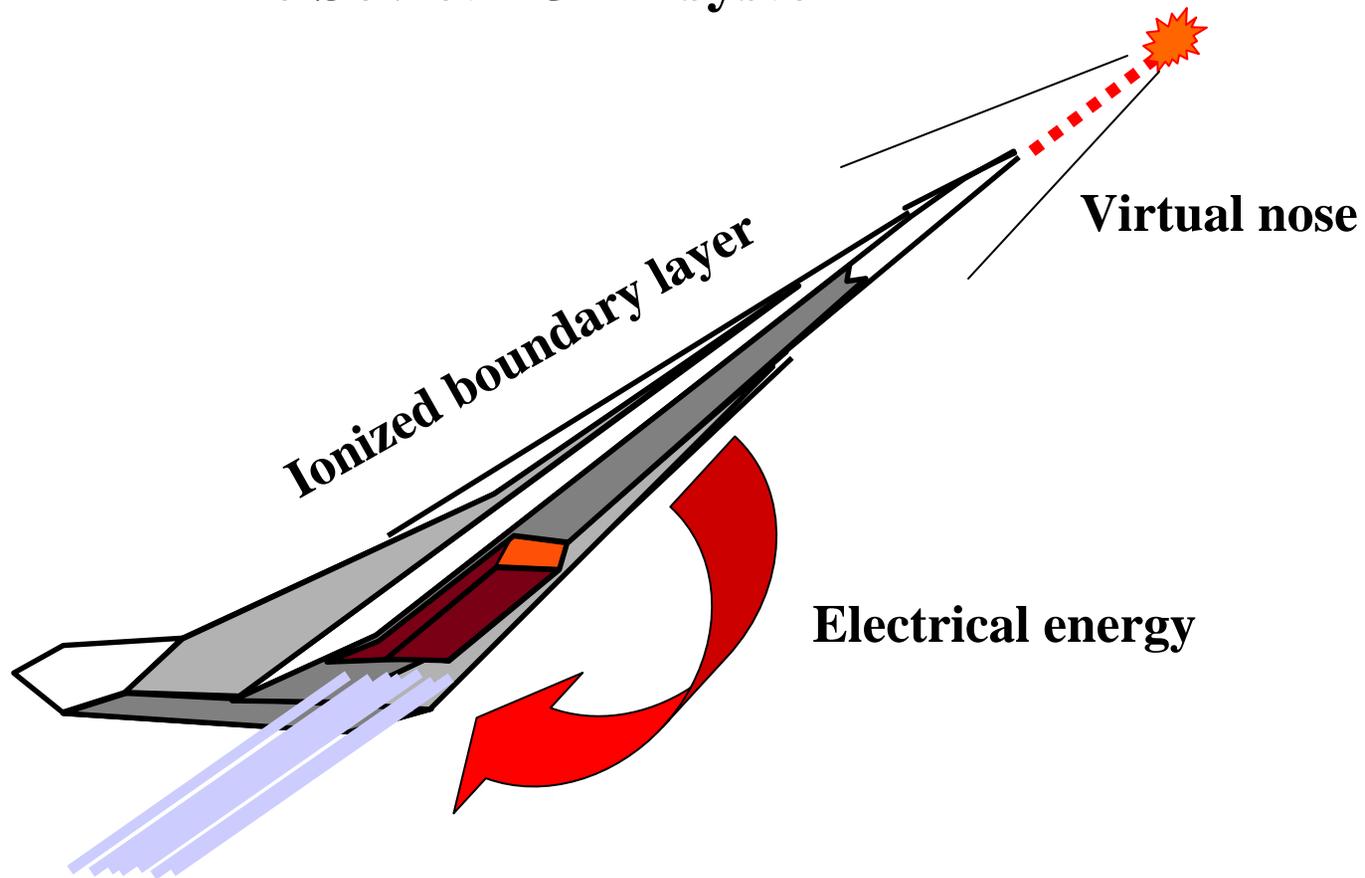
A jumbo to space? Yes, but how?



Limits to airbreathing propulsion

Electricity; Magnetohydrodynamics

The Soviet AJAX system



Magnetohydrodynamic airbreathing vehicle

Most powerful of all engines



Humming bird 300 W/kg.



Gripen 2500 W/kg.



**Ariane
20000 W/kg.**



Insect 60 W/kg.



Man 3 W/kg.